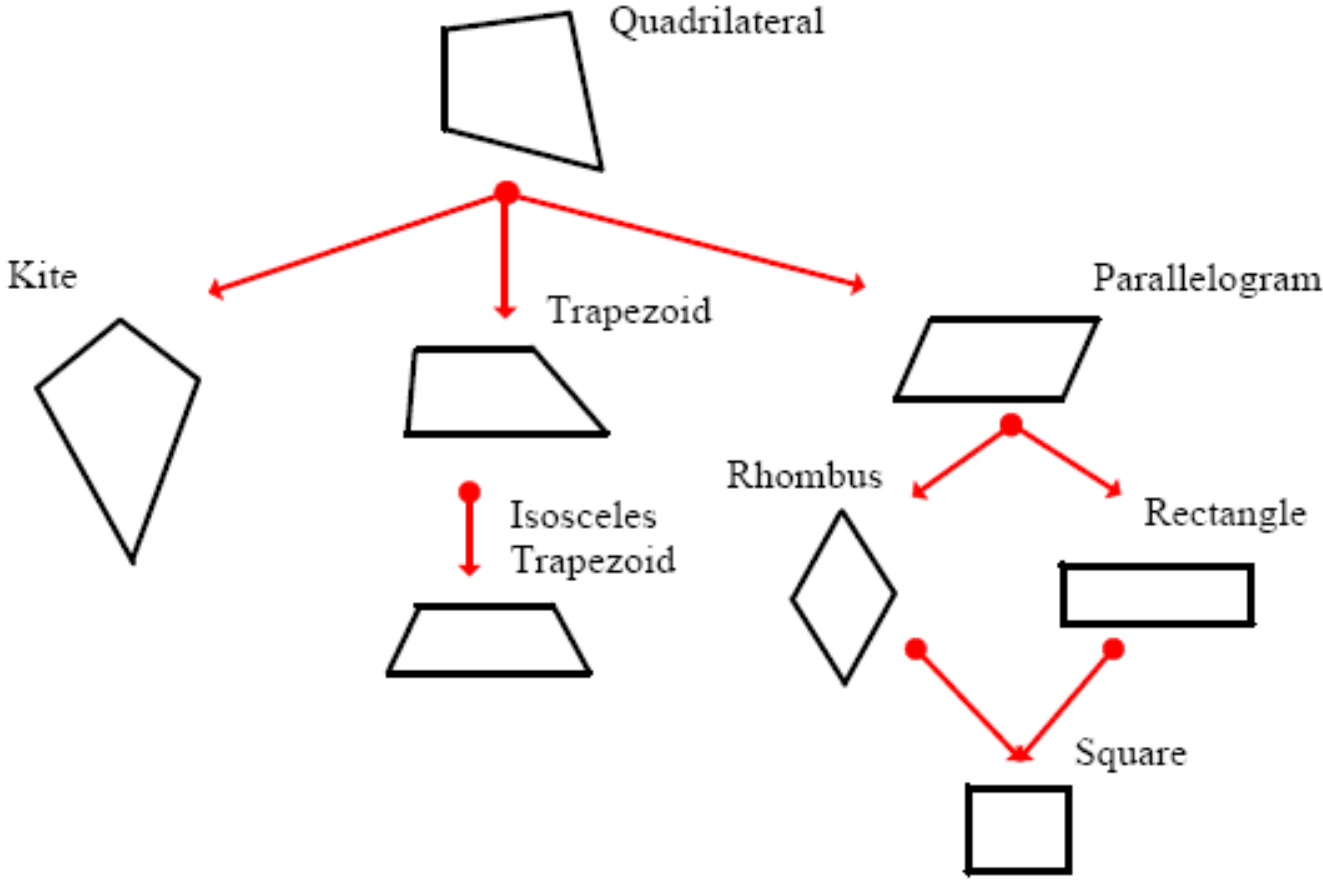


Polygons, Quadrilaterals, and Special Parallelograms



Name: _____ Date: _____ Per: _____

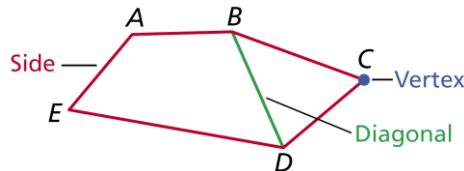
Chapter 6 (Section 1) – Day 1

Angles in polygons

Homework: pg 386 #3 – 41 (odd)

A polygon is a closed plane figure formed by three or more segments that intersect only at their endpoints.

Each segment that forms a polygon is a **side of the polygon**. The common endpoint of two sides is a **vertex of the polygon**. A segment that connects any two nonconsecutive vertices is a **diagonal**.

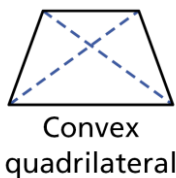


You can name a polygon by the number of its sides. The table shows the names of some common polygons.

Number of Sides	Name of Polygon
3	Triangle
4	Quadrilateral
5	Pentagon
6	Hexagon
7	Heptagon
8	Octagon
9	Nonagon
10	Decagon
12	Dodecagon
n	n -gon

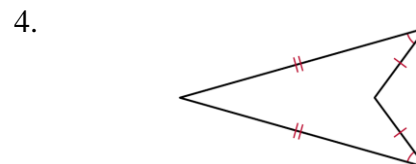
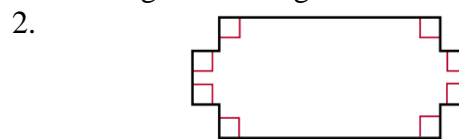
All the sides are congruent in an equilateral polygon. All the angles are congruent in an equiangular polygon. A **regular polygon** is one that is both equilateral and equiangular. If a polygon is not regular, it is called irregular.

A polygon is **concave** if any part of a diagonal contains points in the exterior of the polygon. If no diagonal contains points in the exterior, then the polygon is **convex**. A regular polygon is always convex.




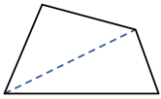
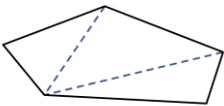
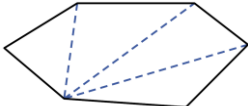
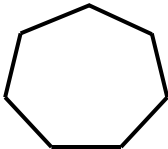
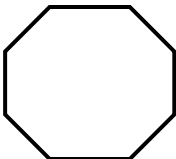
Warm – Up

Tell whether the following polygons are concave or convex and regular or irregular.



Angles in Polygons

Fill in the accompanying table.

Polygon	Number of Sides	Number of Triangles	Sum of Interior Angle Measures
 Triangle	3	1	180°
 Quadrilateral	4	2	$2 \times 180 = 360^\circ$
 Pentagon			
 Hexagon			
 Heptagon			
 Octagon			

Look for a pattern in the table. Write a rule for finding the sum of the measures of the interior angles of a polygon with n sides.

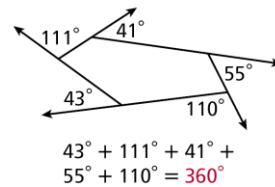
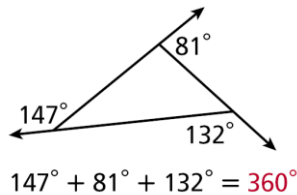
Examples:

1. Find the sum of the interior angles of a decagon.

2. What is the measure of each angle in a regular octagon?

Exterior Angles

Refer to the two polygons below. What do you notice about the exterior angles of any polygon?



Theorem 6.2 **Polygon Exterior Angles Sum** For Your **FOLDABLE**

The sum of the exterior angle measures of a convex polygon, one angle at each vertex, is 360.

Example
 $m\angle 1 + m\angle 2 + m\angle 3 + m\angle 4 + m\angle 5 + m\angle 6 = 360$

The diagram shows a hexagon with exterior angles labeled 1 through 6. Each exterior angle is formed by extending one side of the polygon.

$$\frac{e}{1} = \frac{360}{n}$$

Examples:

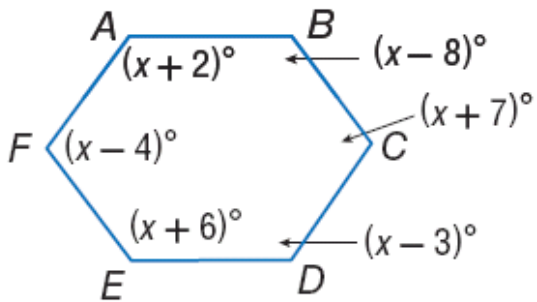
3. Find the measure of each exterior angle of a polygon with 18 sides.

4. The measure of an exterior angle of a convex regular polygon is 36° . Find the number of sides of the polygon.

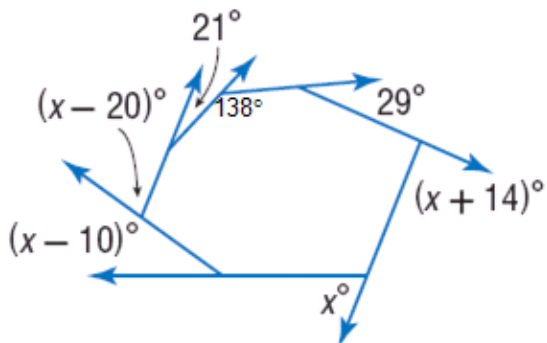
5. How many sides does a regular polygon have if each interior angle measures 160° ?

6. The sum of the interior angles of a convex regular polygon measure 1980° , how many sides does the polygon have?

7. Find the value of x .



8. Find x :



Summary

Properties and Attributes of Polygons

Lesson 6-1

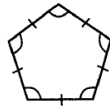
Why? Understanding properties of polygons and their angle sums is fundamental to successful work with quadrilaterals.

Remember

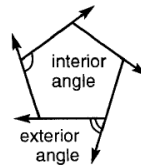
A polygon is *convex* if a segment connecting any two points in the interior of the polygon is completely in the interior.



A polygon that is not convex is *concave*.



A *regular* polygon is equilateral and equiangular.



Theorem

The sum of the interior angle measures of a convex polygon with n sides

$$S_i = (n - 2)180$$

Theorem

The sum of the exterior angle measures, one angle at each vertex, of a convex polygon is 360° .

$$S_e = 360 \text{ (always - no matter what the polygon)}$$

Theorem

$$\text{Interior Angle} + \text{Exterior Angle} = 180^\circ$$

Theorem

$$\frac{e}{1} = \frac{360}{n}$$

Homework

GUIDED PRACTICE

1. **Vocabulary** Explain why an equilateral polygon is not necessarily a *regular* polygon.

Tell whether each outlined shape is a polygon. If it is a polygon, name it by the number of its sides.

2.



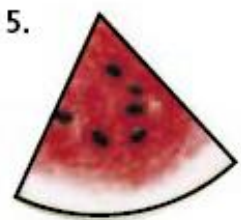
3.



4.

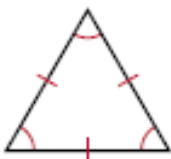


5.

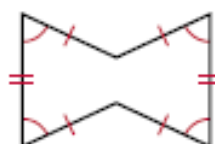


Tell whether each polygon is regular or irregular. Tell whether it is concave or convex.

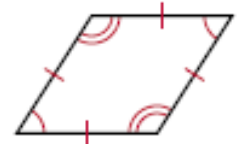
6.



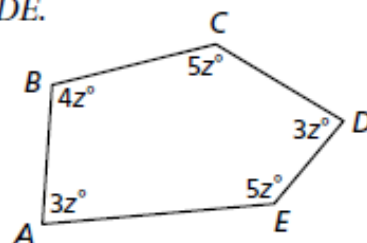
7.



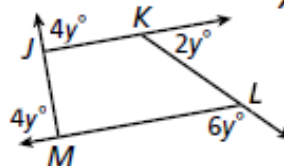
8.



9. Find the measure of each interior angle of pentagon $ABCDE$.
10. Find the measure of each interior angle of a regular dodecagon.
11. Find the sum of the interior angle measures of a convex 20-gon.

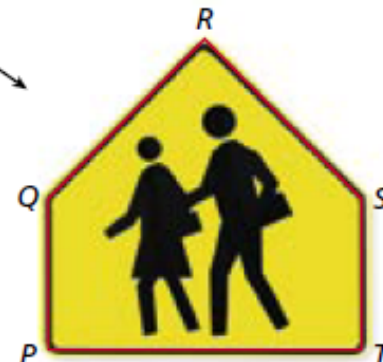


12. Find the value of y in polygon $JKLM$.
13. Find the measure of each exterior angle of a regular pentagon.



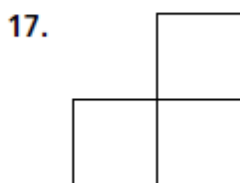
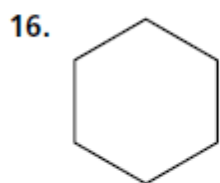
Safety Use the photograph of the traffic sign for Exercises 14 and 15.

14. Name the polygon by the number of its sides.
15. In the polygon, $\angle P$, $\angle R$, and $\angle T$ are right angles, and $\angle Q \cong \angle S$. What are $m\angle Q$ and $m\angle S$?

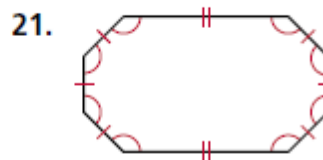
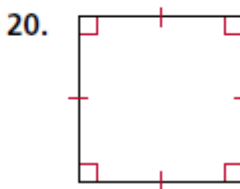
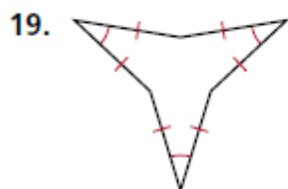


PRACTICE AND PROBLEM SOLVING

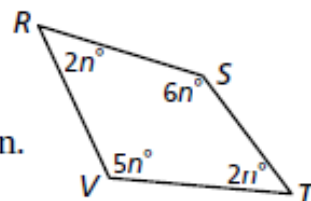
Tell whether each figure is a polygon. If it is a polygon, name it by the number of its sides.



Tell whether each polygon is regular or irregular. Tell whether it is concave or convex.

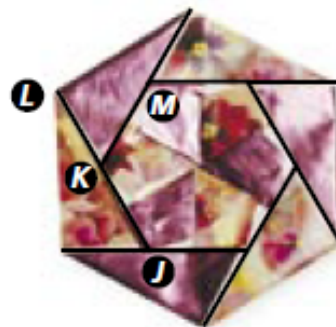


22. Find the measure of each interior angle of quadrilateral $RSTV$.
23. Find the measure of each interior angle of a regular 18-gon.
24. Find the sum of the interior angle measures of a convex heptagon.
25. Find the measure of each exterior angle of a regular nonagon.
26. A pentagon has exterior angle measures of $5a^\circ$, $4a^\circ$, $10a^\circ$, $3a^\circ$, and $8a^\circ$. Find the value of a .



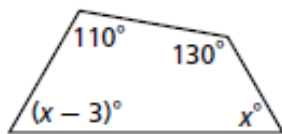
Crafts The folds on the lid of the gift box form a regular hexagon. Find each measure.

27. $m\angle JKM$
28. $m\angle MKL$

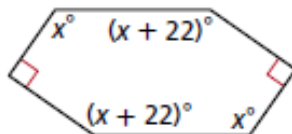


Algebra Find the value of x in each figure.

29.



30.



31.



Find the number of sides a regular polygon must have to meet each condition.

32. Each interior angle measure equals each exterior angle measure.
33. Each interior angle measure is four times the measure of each exterior angle.
34. Each exterior angle measure is one eighth the measure of each interior angle.

Name the convex polygon whose interior angle measures have each given sum.

35. 540°

36. 900°

37. 1800°

38. 2520°

Multi-Step An exterior angle measure of a regular polygon is given. Find the number of its sides and the measure of each interior angle.

39. 120°

40. 72°

41. 36°

42. 24°

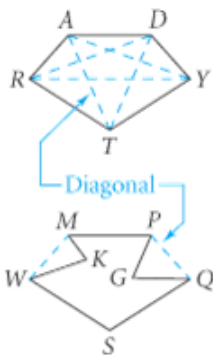
Name: _____

Date: _____ Per: _____

Chapter 6 (section 1) – Day 2

Angles in Polygons

Polygons are classified as convex or concave.



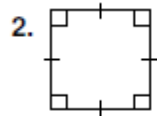
A **convex polygon** has no diagonal with points outside the polygon.

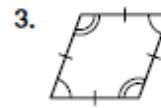
A **concave polygon** has at least one diagonal with points outside the polygon.

Number of Sides	Polygon
3	triangle
4	quadrilateral
5	pentagon
6	hexagon
7	heptagon
8	octagon
9	nonagon
10	decagon
12	dodecagon
n	n -gon

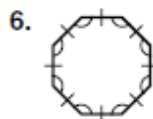
Tell whether each polygon is regular or irregular. Then tell whether it is concave or convex.

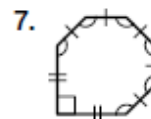




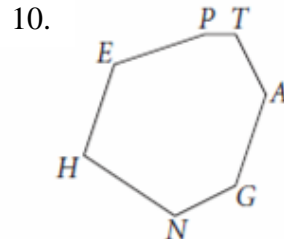
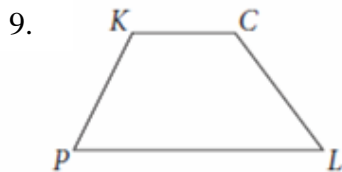
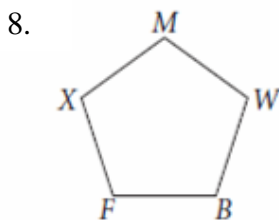








Name each polygon by its vertices.



EXAMPLE Finding a Polygon Angle Sum

Find the sum of the measures of the angles of a 15-gon.

For a 15-gon, $n = 15$.

$$\begin{aligned}
 \text{Sum} &= (n - 2)180 && \text{Polygon Angle-Sum Theorem} \\
 &= (15 - 2)180 && \text{Substitute.} \\
 &= 13 \cdot 180 && \text{Simplify.} \\
 &= 2340
 \end{aligned}$$

The sum of the measures of the angles of a 15-gon is 2340.

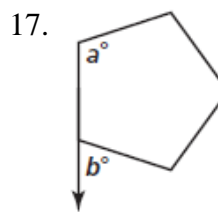
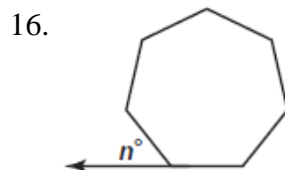
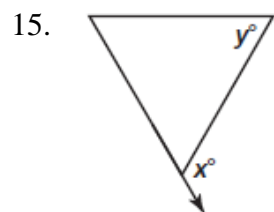
Find the sum of the measures of the interior angles of each convex polygon.

11. 11-gon

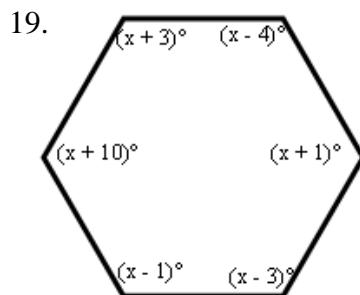
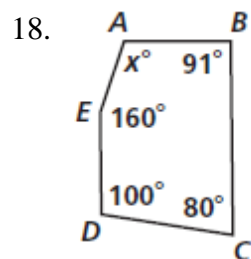
12. 2. 14-gon

14. 3. 17-gon

Find the values of the variables for each polygon. Each is a regular polygon.



Find the value of x .



Not drawn to scale.

Find the measures of an exterior angle given the number of sides of each regular polygon.

20. 16

21. 24

23. 30

The measure of an interior angle of a regular polygon is given. Find the number of sides in the polygon.

24. 144

25. 156

26. 160

The sum of the measures of the angles of a polygon with n sides is given. Find n .

27. 2160°

28. 2880°

29. 5760°

Name: _____ Date: _____ per: _____

Chapter 6 (Section 2) – Day 3

Parallelograms

Homework: Worksheet

Properties of Parallelograms

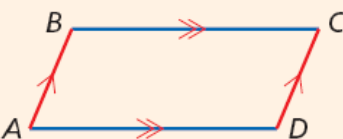
Lesson 6-2

Properties of Parallelograms

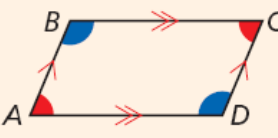
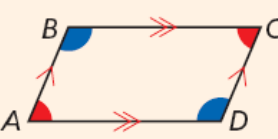
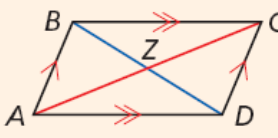
In a parallelogram,

1. The opposite sides are parallel by definition.
2. The opposite sides are congruent.
3. The opposite angles are congruent.
4. The diagonals bisect each other.
5. Any pair of consecutive angles are supplementary.
6. Each diagonal separates it into two congruent triangles.

Theorem 6-2-1 Properties of Parallelograms

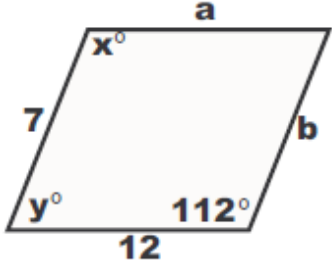
THEOREM	HYPOTHESIS	CONCLUSION
If a quadrilateral is a parallelogram, then its opposite sides are congruent. (□ → opp. sides ≅)		$\overline{AB} \cong \overline{CD}$ $\overline{BC} \cong \overline{DA}$

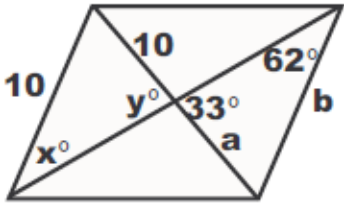
Theorems Properties of Parallelograms

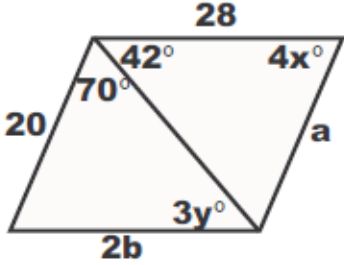
THEOREM	HYPOTHESIS	CONCLUSION
6-2-2 If a quadrilateral is a parallelogram, then its opposite angles are congruent. (□ → opp. ∠ ≅)		$\angle A \cong \angle C$ $\angle B \cong \angle D$
6-2-3 If a quadrilateral is a parallelogram, then its consecutive angles are supplementary. (□ → cons. ∠ supp.)		$m\angle A + m\angle B = 180^\circ$ $m\angle B + m\angle C = 180^\circ$ $m\angle C + m\angle D = 180^\circ$ $m\angle D + m\angle A = 180^\circ$
6-2-4 If a quadrilateral is a parallelogram, then its diagonals bisect each other. (□ → diags. bisect each other)		$\overline{AZ} \cong \overline{CZ}$ $\overline{BZ} \cong \overline{DZ}$

Level A:

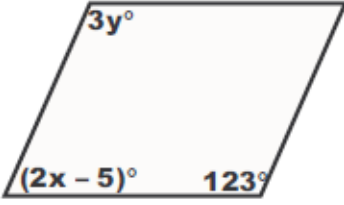
In exercises 14 – 16, each quadrilateral is a parallelogram. Find the indicated values.

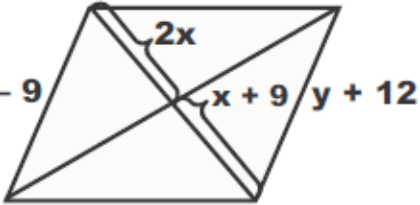
<p>14. $a =$ _____ $b =$ _____ $x =$ _____ $y =$ _____</p>	
---	---

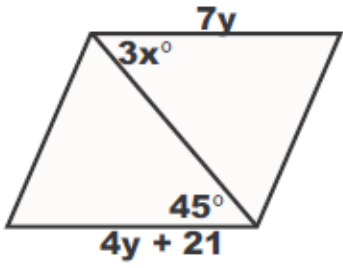
<p>15. $a =$ _____ $b =$ _____ $x =$ _____ $y =$ _____</p>	
---	---

<p>16. $a =$ _____ $b =$ _____ $x =$ _____ $y =$ _____</p>	
---	--

In exercises 17 – 19, what values must 'x' and 'y' have to make each quadrilateral a parallelogram?

<p>17. $x =$ _____ $y =$ _____</p>	
---	---

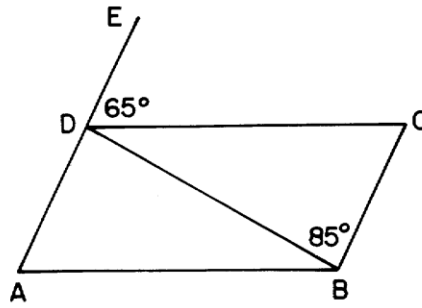
<p>18. $x =$ _____ $y =$ _____</p>	
---	---

<p>19. $x =$ _____ $y =$ _____</p>	
---	---

Level B

20.

In the accompanying diagram of parallelogram $ABCD$, side \overline{AD} is extended through D to E and \overline{DB} is a diagonal. If $m\angle EDC = 65$ and $m\angle CBD = 85$, find $m\angle CDB$.



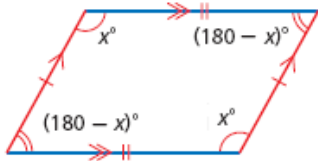
21. In parallelogram $LMNO$, an exterior angle at vertex O measures 72° . Find the measure, in degrees, of $\angle L$.

Summary

Properties of Parallelograms

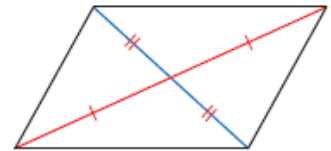
Lesson 6-2

Why? The properties of parallelograms make these figures useful in mechanics and construction.



A quadrilateral is a parallelogram \rightarrow all of these properties are true.

- Opposite sides are parallel.
- Opposite sides are congruent.
- Opposite angles are congruent.
- Consecutive angles are supplementary.
- Diagonals bisect each other.



Name: _____ Date: _____ per: _____

Chapter 6 (section 4) – Day 4

Special Parallelograms

Homework: Worksheet

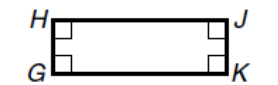
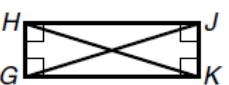
Rectangles

Definition: A **rectangle** is a parallelogram with one right angle.



Properties of a Rectangle

1. A rectangle has all the properties of a parallelogram.
2. A rectangle contains four right angles and is therefore equiangular.
3. The diagonals of a rectangle are congruent.

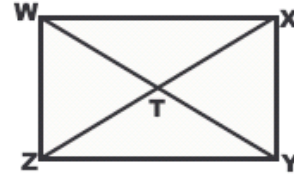
Properties of Rectangles	
 <p>$GHJK$ is a parallelogram.</p> <p>If a quadrilateral is a rectangle, then it is a parallelogram.</p>	 <p>$\overline{GJ} \cong \overline{HK}$</p> <p>If a parallelogram is a rectangle, then its diagonals are congruent.</p>

Since a rectangle is a parallelogram, a rectangle also has all the properties of parallelograms.

PART 3. RECTANGLES

Quadrilateral WXYZ is a rectangle. Use this rectangle for problems 20 – 22.

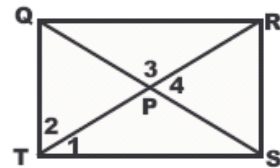
_____ 20.	If $WY = 19$, then $ZX = ?$
_____ 21.	If $WY = 19$, then $WT = ?$
_____ 22.	If $TX = 4.5$, then $WY = ?$



_____ 23.	Rectangle GALS has diagonals \overline{GL} and \overline{AS} . If $GL = 3a + 6$ and $AS = 5a - 18$, then $a = ?$
_____ 24.	Rectangle BOYS has diagonals \overline{BY} and \overline{OS} , which intersect at X. If $m\angle XOB = 70^\circ$, then $m\angle YSO = ?$ and $m\angle BSO = ?$

Use rectangle QRST and the given information to solve problems 25 – 26.

_____ 25.	$QP = 6$, find RT .
_____ 26.	$QT = 8$, find RS .

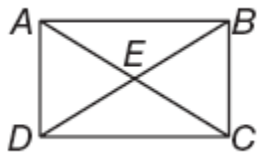


Solve each of the following.

_____ 27.	In rectangle RAIN below, $YR = 3x$ and $NY = 18$, find 'x'.
_____ 28.	$m\angle 1 = 55^\circ$, find the measures of $\angle 2$, $\angle 3$ and $\angle 4$.
_____ 29.	$m\angle 3 = 110^\circ$, find the measures of $\angle 1$, $\angle 2$, and

Practice Problems

- a. If $AE = 5$, $BC = 6$, and $DC = 8$, find AC , BD , AD , and AB .



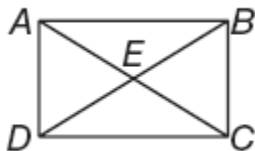
$AC = \underline{\hspace{2cm}}$

$BD = \underline{\hspace{2cm}}$

$AD = \underline{\hspace{2cm}}$

$AB = \underline{\hspace{2cm}}$

- b. If $BD = 3x - 7$ and $CA = x + 5$, find BD , ED , CA , and AE .



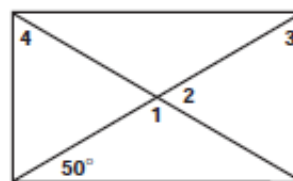
$BD = \underline{\hspace{2cm}}$

$ED = \underline{\hspace{2cm}}$

$CA = \underline{\hspace{2cm}}$

$AE = \underline{\hspace{2cm}}$

- c. Find the measures of the numbered angles in each rectangle.



$m \angle 1 = \underline{\hspace{2cm}}^\circ$

$m \angle 2 = \underline{\hspace{2cm}}^\circ$

$m \angle 3 = \underline{\hspace{2cm}}^\circ$

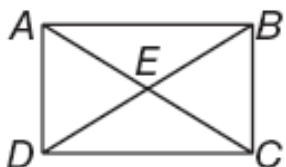
$m \angle 1 = \underline{\hspace{2cm}}^\circ$

$m \angle 2 = \underline{\hspace{2cm}}^\circ$

$m \angle 3 = \underline{\hspace{2cm}}^\circ$

$m \angle 4 = \underline{\hspace{2cm}}^\circ$

- d. If $m \angle DAC = 2x + 4$ and $m \angle BAC = 3x + 1$, find $m \angle BAC$.



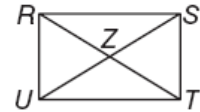
Homework

NAME _____ DATE _____ PERIOD _____

6-4 Practice

Rectangles

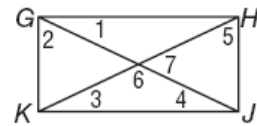
ALGEBRA Quadrilateral $RSTU$ is a rectangle.



1. If $UZ = x + 21$ and $ZS = 3x - 15$, find US .
2. If $RZ = 3x + 8$ and $ZS = 6x - 28$, find UZ .
3. If $RT = 5x + 8$ and $RZ = 4x + 1$, find ZT .
4. If $m\angle SUT = 3x + 6$ and $m\angle RUS = 5x - 4$, find $m\angle SUT$.
5. If $m\angle SRT = x + 9$ and $m\angle UTR = 2x - 44$, find $m\angle UTR$.
6. If $m\angle RSU = x + 41$ and $m\angle TUS = 3x + 9$, find $m\angle RSU$.

Quadrilateral $GHJK$ is a rectangle. Find each measure if $m\angle 1 = 37$.

- | | |
|-----------------|-----------------|
| 7. $m\angle 2$ | 8. $m\angle 3$ |
| 9. $m\angle 4$ | 10. $m\angle 5$ |
| 11. $m\angle 6$ | 12. $m\angle 7$ |



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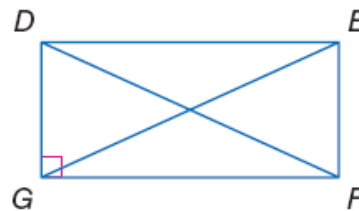
Chapter 6 (Section 4) – Day 5

Special Parallelograms

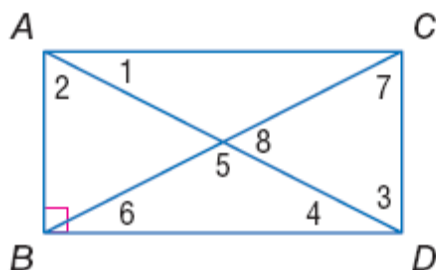
Homework: Worksheet

Warm - Up

1. Quadrilateral $DEFG$ is a rectangle.
If $FD = 3x - 7$ and $EG = x + 5$, find EG .



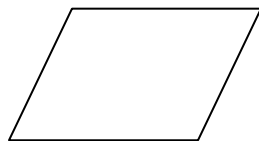
2. Quadrilateral $ABCD$ is a rectangle. Find each measure if $m\angle 2 = 40$.



$m\angle 1 = \underline{\hspace{1cm}}^\circ$	$m\angle 5 = \underline{\hspace{1cm}}^\circ$
$m\angle 2 = 40^\circ$	$m\angle 6 = \underline{\hspace{1cm}}^\circ$
$m\angle 3 = \underline{\hspace{1cm}}^\circ$	$m\angle 7 = \underline{\hspace{1cm}}^\circ$
$m\angle 4 = \underline{\hspace{1cm}}^\circ$	$m\angle 8 = \underline{\hspace{1cm}}^\circ$

Rhombus

Definition: A **rhombus** is a parallelogram with 2 congruent consecutive sides.

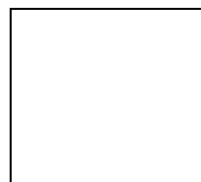


Properties of a Rhombus

1. A rhombus has all the properties of a parallelogram.
2. A rhombus is equilateral.
3. The diagonals of a rhombus are perpendicular to each other.
4. The diagonals of a rhombus bisect its angles.

Square

Definition: A **square** is a rectangle with 2 congruent consecutive sides.

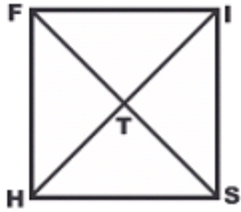


Properties of a Square

1. A square has all the properties of a rectangle.
2. A square has all the properties of a rhombus.

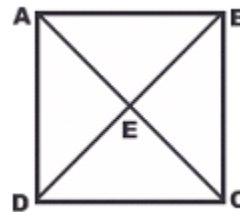
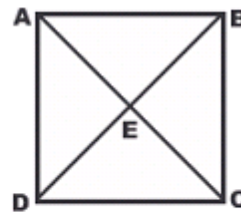
PART 4. SQUARES & RHOMBI

Find the indicated measure.

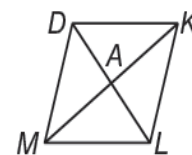
<p>_____ 30.</p>	<p>FISH is a square with $IT = 6$. Find IH and IS.</p>	
<p>_____ 31.</p>	<p>If MNOP is a square, what is $m\angle MNP$?</p>	

Use square ABCD and the given information to find each value.

<p>_____ 32.</p>	<p>If $m\angle AEB = (3x)^\circ$, find 'x'.</p>
<p>_____ 33.</p>	<p>If $m\angle BAC = (9x)^\circ$, find 'x'.</p>
<p>_____ 34.</p>	<p>If $AB = 2x + 4$ and $CD = 3x - 5$, find BC. Find BC and BD.</p>
<p>_____ a.</p>	<p>The perimeter of the square is 32 cm. Find the length of diagonal DB.</p>
<p>_____ b.</p>	<p>$DE = 10$, find AD.</p>
<p>_____ c.</p>	<p>The area of the square is 16. Find EC.</p>



Find the indicated value.



_____ 35.	ACKJ is a rhombus. $AC = 6y + 4$, $CK = 5y + 8$, and $KJ = 3y + 16$. Find the value of 'y'.
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_____ a.	<p>Quadrilateral <i>DKLM</i> is a rhombus.</p> <p>If $DK = 8$, find KL.</p>
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_____ b.	<p>Quadrilateral <i>DKLM</i> is a rhombus.</p> <p>If $DA = 4x$ and $AL = 5x - 3$, find DL.</p>
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_____ c.	The diagonals of a Rhombus are 10, and 24 cm. Find the length of the side of the rhombus.
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$m\angle 1 = \underline{\hspace{1cm}}^\circ$ $m\angle 2 = \underline{\hspace{1cm}}^\circ$ $m\angle 3 = \underline{\hspace{1cm}}^\circ$ $m\angle 4 = \underline{\hspace{1cm}}^\circ$	<p>Find the measures of the numbered angles in each rhombus.</p> <p>A rhombus with a diagonal from the top vertex to the bottom vertex. The top-left interior angle is labeled 1, the bottom-left interior angle is labeled 2, the top-right interior angle is labeled 3, and the bottom-right interior angle is labeled 4. The bottom-right interior angle is also labeled 104°.</p>
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$m\angle 1 = \underline{\hspace{1cm}}^\circ$ $m\angle 2 = \underline{\hspace{1cm}}^\circ$ $m\angle 3 = \underline{\hspace{1cm}}^\circ$ $m\angle 4 = \underline{\hspace{1cm}}^\circ$	<p>Find the measures of the numbered angles in each rhombus.</p> <p>A rhombus with both diagonals. The top-left interior angle is labeled 1, the top-right interior angle is labeled 2, the bottom-right interior angle is labeled 3, and the bottom-left interior angle is labeled 4. The bottom-right interior angle is also labeled 58°.</p>
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Homework

Properties of the Rectangle, Rhombus, and Square

Rectangle

all properties of parallelograms
plus
—all diagonals are congruent
—all angles measure 90°

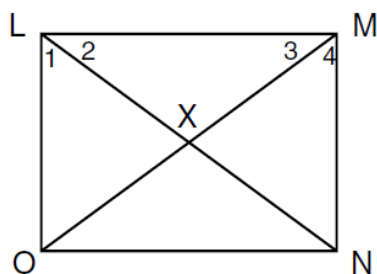
Rhombus

all properties of parallelograms
plus
—all sides are congruent
—all diagonals are perpendicular
—all diagonals bisect opposite angles

Square

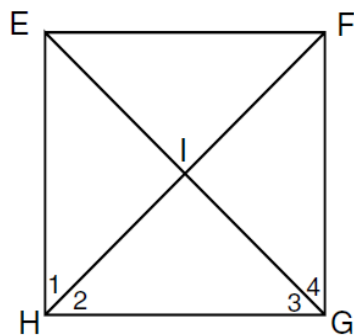
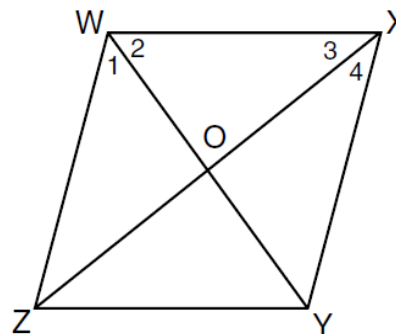
all properties of
—parallelogram
—rectangle
—rhombus

Use the properties to solve for the missing measures in the diagrams.



1. LMNO is a rectangle. If $LM = 16$, $MN = 12$, and $\angle 1 = 60^\circ$, find the following:
- | | | |
|-----------------|-------------------------|-----------------------|
| a. $ON =$ _____ | d. $LX =$ _____ | g. $OX =$ _____ |
| b. $OL =$ _____ | e. $\angle LON =$ _____ | h. $\angle 3 =$ _____ |
| c. $LN =$ _____ | f. $\angle 2 =$ _____ | i. $\angle 4 =$ _____ |

2. WXYZ is a rhombus. If $WX = 4$ and $\angle WXY = 60^\circ$, find the following:
- | | | |
|-------------------------|-----------------------|-----------------|
| a. $XY =$ _____ | d. $\angle 2 =$ _____ | g. $WO =$ _____ |
| b. $\angle ZWX =$ _____ | e. $\angle 3 =$ _____ | h. $OX =$ _____ |
| c. $\angle 1 =$ _____ | f. $\angle 4 =$ _____ | i. $WY =$ _____ |



3. EFGH is a square. If $EF = 10$, find the following:
- | | | |
|-------------------------|-------------------------|-----------------------|
| a. $FG =$ _____ | d. $EI =$ _____ | g. $\angle 1 =$ _____ |
| b. $\angle EFG =$ _____ | e. $IF =$ _____ | h. $\angle 3 =$ _____ |
| c. $EG =$ _____ | f. $\angle EIF =$ _____ | i. $HF =$ _____ |

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Chapter 6 (Section 6) – Day 6

Trapezoids

Homework: Worksheet

Warm - Up

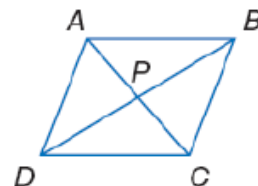
1. $ABCD$ is a rhombus. If $PB = 12$, $AB = 15$, and $m\angle ABD = 24$, find each measure.

23. AP

25. $m\angle BDA$

24. CP

26. $m\angle ACB$



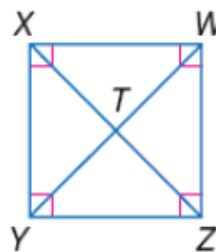
2. $WXYZ$ is a square. If $WT = 3$, find each measure.

27. ZX

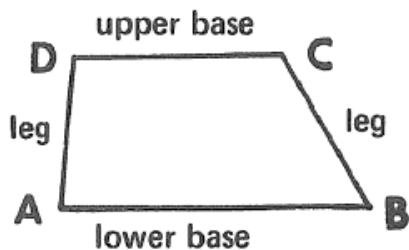
29. $m\angle WTZ$

28. XY

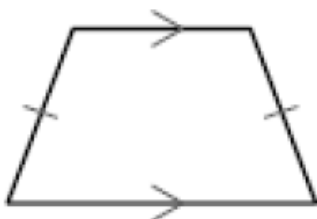
30. $m\angle WYX$



Definition: A **trapezoid** is a quadrilateral with one pair of parallel sides.



Definition: An **Isosceles trapezoid** is a trapezoid with non parallel sides congruent.



- In an isosceles trapezoid, each pair of base angles is congruent.
- If a trapezoid has one pair of congruent base angles, then it is isosceles.
- A trapezoid is isosceles if and only if its diagonals are congruent.

Theorems

Isosceles Trapezoids

For Your

FOLDABLE

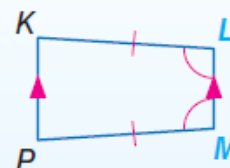
6.21 If a trapezoid is isosceles, then each pair of base angles is congruent.

Example If trapezoid $FGHJ$ is isosceles, then $\angle G \cong \angle H$ and $\angle F \cong \angle J$.



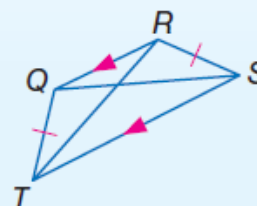
6.22 If a trapezoid has one pair of congruent base angles, then it is an isosceles trapezoid.

Example If $\angle L \cong \angle M$, then trapezoid $KLMP$ is isosceles.



6.23 A trapezoid is isosceles if and only if its diagonals are congruent.

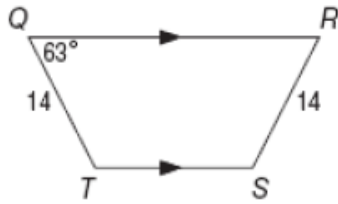
Example If trapezoid $QRST$ is isosceles, then $\overline{QS} \cong \overline{RT}$. Likewise, if $\overline{QS} \cong \overline{RT}$, then trapezoid $QRST$ is isosceles.



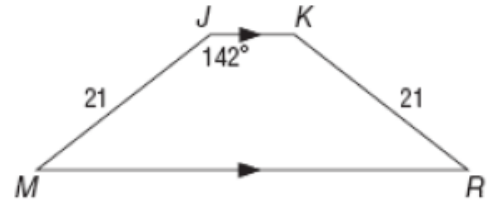
Practice Problems

ALGEBRA Find each measure.

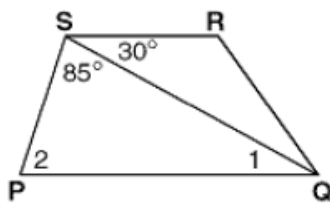
1. $m\angle S$



2. $m\angle M$



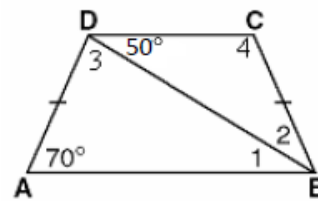
3. Trapezoid PQRS. Find the $m\angle 1$ and $\angle 2$.



$m\angle 1 = \underline{\hspace{2cm}}^\circ$

$m\angle 2 = \underline{\hspace{2cm}}^\circ$

4. Isosceles Trapezoid ABCD.



$m\angle 1 = \underline{\hspace{2cm}}^\circ$

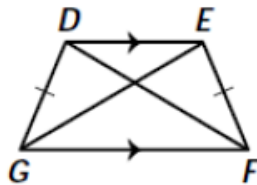
$m\angle 2 = \underline{\hspace{2cm}}^\circ$

$m\angle 3 = \underline{\hspace{2cm}}^\circ$

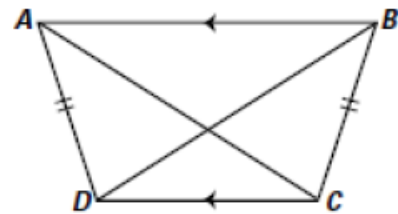
$m\angle 4 = \underline{\hspace{2cm}}^\circ$

5. Find the values of the variables.

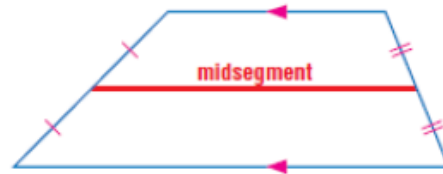
$DF = 4x, EG = 2x + 16$



6. $AC = 7x - 15, BD = 4x + 15$



The **midsegment of a trapezoid** is the segment that connects the midpoints of the legs of the trapezoid. The theorem below relates the midsegment and the bases of a trapezoid.



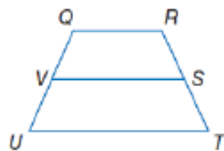
$$2m = b_1 + b_2$$

- The midsegment of a trapezoid is parallel to each base. $\overline{AB} \parallel \overline{MN}$ and $\overline{AB} \parallel \overline{LP}$
- The length of the midsegment is one-half the sum of the length of the bases.

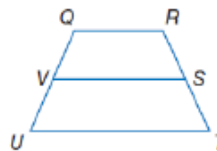
$$AB = \frac{1}{2}(MN + LP)$$

For trapezoid $QRTU$, V and S are midpoints of the legs.

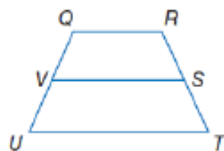
7. If $QR = 12$ and $UT = 22$, find VS .



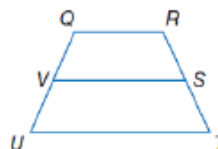
8. If $QR = 4$ and $UT = 16$, find VS .



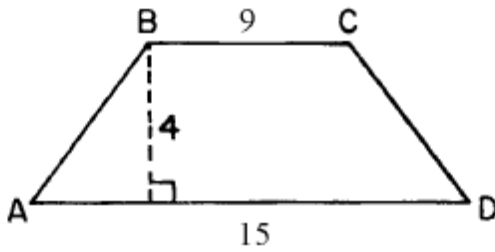
9. If $VS = 9$ and $UT = 12$, find QR .



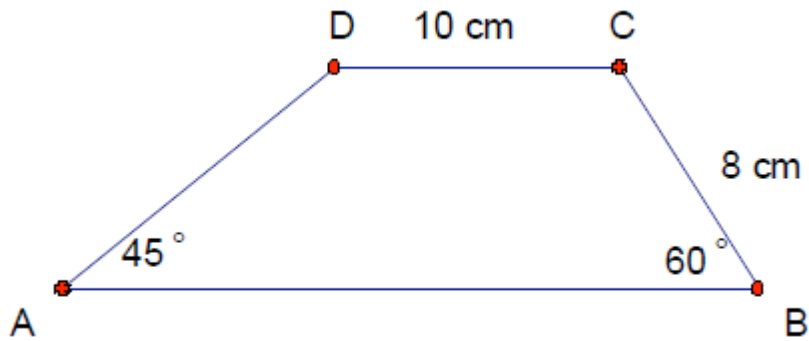
10. If $RQ = 3x - 3$, $UT = 4x + 2$, and $VS = 10$, find VS .



11. In the accompanying figure, isosceles trapezoid $ABCD$ has bases of lengths 9 and 15 and an altitude of length 4. Find AB .

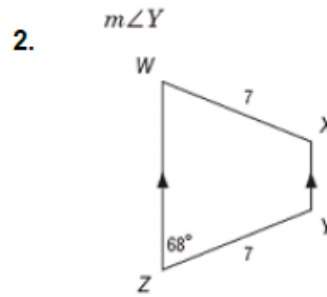
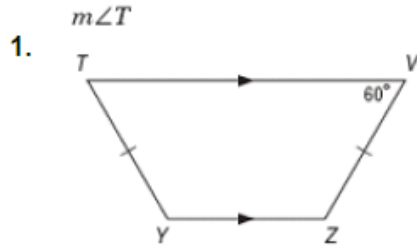


12. Find the length of base \overline{AB} of trapezoid $ABCD$.

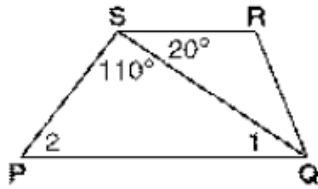


Homework – Trapezoids

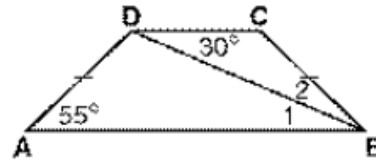
Find each measure.



3. Trapezoid PQRS. Find the $m\angle 1$ and $\angle 2$.

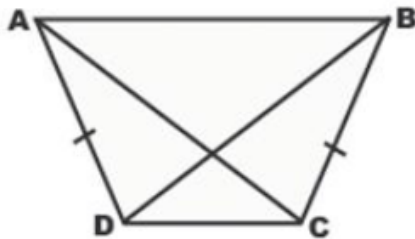


4. ABCD is an isosceles trapezoid. Find the $m\angle 1$ and $\angle 2$.

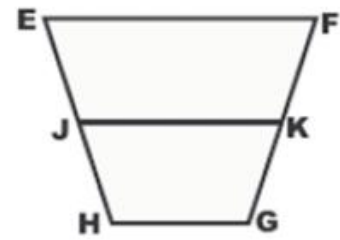


5. MATH is an isosceles trapezoid with $\overline{AT} \parallel \overline{MH}$. If $m\angle M = (3x - 9)^\circ$ and $m\angle H = (x + 3)^\circ$, find the value of 'x'.

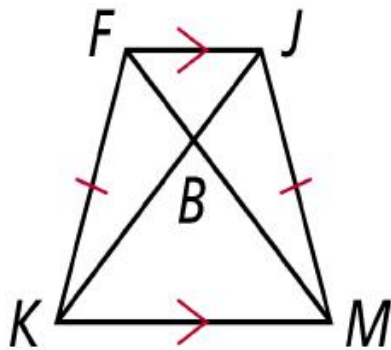
6. Let $AC = 25$ and $DB = 5x$.



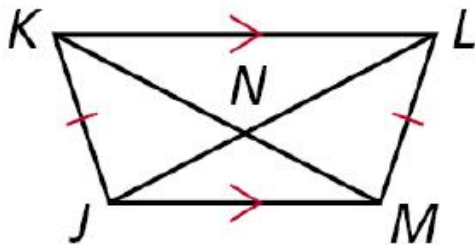
7. If $EH = FG$, and $m\angle E = 65^\circ$, then $m\angle G = ?$
and $m\angle GKJ = ?$



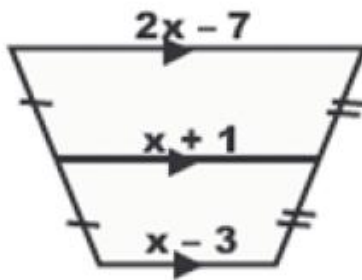
8. $KB = 12$ and $MF = 30$. Find FB .



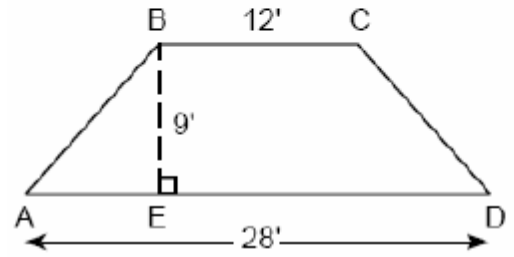
9. $JN = 10$, and $NL = 14$. Find KM .



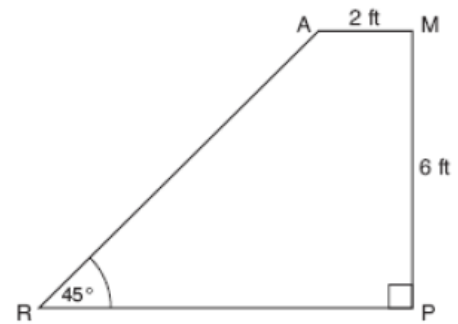
10. Find the value of x .



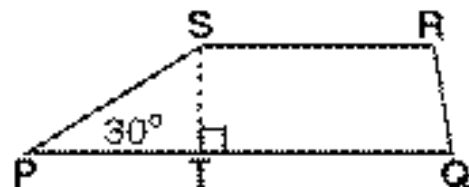
11. The cross section of an attic is in the shape of an isosceles trapezoid, as shown in the accompanying figure. If the height of the attic is 9 feet, $BC = 12$ feet, and $AD = 28$ feet, find the length of \overline{AB} to the nearest foot.



12. The accompanying diagram shows ramp \overline{RA} leading to level platform \overline{AM} , forming an angle of 45° with level ground. If platform \overline{AM} measures 2 feet and is 6 feet above the ground. Find RA .



13. If $PQ = 15$, and $SR = 9$, find ST and PS .



The Quadrilateral Family

